

# Managing Capital Flows in the Presence of External Risks

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*The views expressed in this presentation are those of the authors and do not necessarily reflect the position of the Federal Reserve Board or the Federal Reserve System.*

# Introduction

## External Risks and Policy

1. External shocks affect economic activity (independent of countries' fundamentals).
  - ▶ Generate large and volatile capital flows and affect the real economy
    - Reminded by Global Financial Crisis
  - ▶ Significant risks: 1st and 2nd moments of world interest rates matter
    - ▶ Data and previous work
2. Policy prescriptions to prevent and reduce the effects of large and volatile capital flows.
  - ▶ Policy makers and international institutions have justified capital account intervention as a response to perceived increase in external risks (**volatility**), e.g. **uncertainty** generated by "Taper Tantrum."

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**IMF (2012):** “Capital flows have grown significantly in both size and **volatility** [...] (these) carry risk. Because capital flows have a bearing on economic and financial stability in both individual economies and globally, an important challenge for policy makers is to develop a coherent approach to capital flows and the policies that affect them.”

# Motivation and Question

## Theoretical Framework: Silent on External Risks

2. ⇒ Theoretical literature on **macroprudential policy in small open economies**  
→ *Benchmark theoretical framework*: Lorenzoni (2008), Bianchi (2010), Jeanne (2012), Korinek and Mendoza (2014)
  - ▶ Pecuniary externalities → overborrowing → scope for intervention based on welfare.
  - ▶ Optimal policy response to domestic (output) shocks.
  - ▶ Financial crises rely on size of capital flows, **not volatility**.

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  - ▶ Environment in which external shocks affect asset prices driving pecuniary externality.

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- **However, literature silent on policy response to shocks to external risk.**
- ▶ Environment in which external shocks affect asset prices driving pecuniary externality.
- **Question**: How should optimal macroprudential policy respond to external shocks (international interest rates)?

# Methodology

## What do we do?

- 1 Study response of optimal policy to shocks to 1st and 2nd moments of international interest rates in a benchmark SOE framework with external borrowing constraints.
  - ▶ Estimate stochastic process for international interest rates with regime-switches in volatility.
- 2 Model: SOE subject to endowment + interest rate shocks and collateral constraint that depends on asset prices:
  - ▶ Endogenous financial crises nested within business cycles; and pecuniary externalities  $\Rightarrow$  ex ante policy intervention
  - ▶ Microfoundation of collateral constraint.
- 3 Numerical analysis of time-consistent optimal policy across interest rate levels and volatility regimes.

# Findings

- 1 Simulations of financial crises the evolution of external shocks are consistent with the data.
  - ▶ Reyes-Heroles and Tenorio (2017)



# Findings

- ① Simulations of financial crises the evolution of external shocks are consistent with the data.
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- ② In the competitive equilibrium, allocations and prices are quantitatively sensitive to external interest rate shocks, but not to their volatility.
- ③ The borrowing decisions that solve the time-consistent constrained efficient allocation depend on the level and volatility of external shocks.
  - ▶ Incidence and severity of crises shape optimal policy → Shocks to volatility affect asset prices.

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- ② In the competitive equilibrium, allocations and prices are quantitatively sensitive to external interest rate shocks, but not to their volatility.
- ③ The borrowing decisions that solve the time-consistent constrained efficient allocation depend on the level and volatility of external shocks.
  - ▶ Incidence and severity of crises shape optimal policy → Shocks to volatility affect asset prices.
- ④ No monotone relation between macroprudential tax on external debt and external shocks.
  - ▶ Tax schedule as a function of current debt does not shift in one single direction when external risks change.
  - ▶ “Volatility paradox” contrary to *conventional wisdom* in policy circles.

## Related Literature

- Capital Flows, Financial Crises and Optimal Policy:
  - ▶ Positive analysis: Mendoza and Smith (2002) and Mendoza (2010).
  - ▶ Optimal policy: Lorenzoni (2008), Jeanne and Korinek (2010), Korinek (2011), Bianchi (2011) Bianchi and Mendoza (2011, 2013, forth), Benigno et al. (2016, 2012), Iacoviello et al. (2016)
  - ▶ Optimal capital controls: Schmitt-Grohé and Uribe (2016a,b)
- Emerging Market Business Cycles and Global Shocks:
  - ▶ Neumeyer and Perri (2005), Uribe and Yue (2006), Fernández-Villaverde et al. (2011)
  - ▶ Mackowiak (2007), Chang and Fernández (2013), Eichengreen and Gupta (2016) [capital reversals]
  - ▶ Sovereign default: Longstaff et al. (2011), Johri et al. (2015)

# The Model

Small open economy subject to collateral constraint [similar to JK(2010) & BM(forth)]

- SOE with an infinitely lived unit continuum of identical households that consume a single traded good  $c_t$ .
  - ▶ Access to international bonds markets and domestic asset markets.
    - Period  $t$  divided into Morning (M), Afternoon (A) and Night (N).
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- Sources of risk:
  - ▶ Stochastic external interest rate  $R_t = R \times \exp(r_t)$ .
  - ▶ Variance of interest rate process depends on regime:  $\sigma_t^r$ .
  - ▶ Stochastic endowment (Lucas tree) pays a dividend  $d_t = d \times \exp(z_t)$ .

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- Financial frictions  $\rightarrow$  Collateral constraint
  - ▶ Fraction  $\kappa$  of value of assets as collateral with foreign lenders.
    - **A**: Households can divert resources and default on existing debt. Lenders do not observe actions. **N**: Lenders sell confiscated asset.
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- Financial crises occur when collateral constraint binds.

# The Model

## Exogenous Shocks

- $(z_t, r_t)'$  follows the VAR specification

$$\begin{pmatrix} z_t \\ r_t \end{pmatrix} = A_0 + A_1 \begin{pmatrix} z_{t-1} \\ r_{t-1} \end{pmatrix} + \begin{pmatrix} \varepsilon_t^z \\ \varepsilon_t^r \end{pmatrix}.$$

- $(\varepsilon_t^z, \varepsilon_t^r)' \sim N(0, \Sigma_t)$  where

$$\Sigma_t = \begin{pmatrix} (\sigma^z)^2 & \rho \cdot \sigma^z \cdot \sigma_t^r \\ \rho \cdot \sigma^z \cdot \sigma_t^r & (\sigma_t^r)^2 \end{pmatrix}.$$

- Regime-switching:  $\sigma_t^r \in \{\sigma_L^r, \sigma_H^r\}$ , with  $0 < \sigma_L^r < \sigma_H^r$ , and switching between regimes governed by first-order Markov process with transition matrix  $\Pi$ .



# The Model

## Household's Problem (implied by no default)

- Given prices, each household solves:

$$\max_{c_t, b_{t+1}, s_{t+1}} \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t u(c_t)$$

subject to

$$c_t + q_t s_{t+1} + \frac{b_{t+1}}{R_t} = (q_t + d_t) s_t + b_t$$
$$-\frac{b_{t+1}}{R_t} \leq \kappa q_t^c s_{t+1},$$

where

- ▶  $b_t$ : face value of bonds held at beginning of period  $t$ .
- ▶  $s_t$ : share of the asset held at the beginning of period  $t$  (only trades domestically).
- ▶  $q_t$ : market value of the asset.
- ▶  $q_t^c$ : price at which collateral is valued at  $N$ . ▶ Derivation of CC

# The Model

## Competitive Equilibrium

### Definition

Sequences  $\{c_t, b_{t+1}, s_{t+1}\}_{t=0}^{\infty}$  for each household, and prices  $\{q_t, q_t^c\}_{t=0}^{\infty}$  such that given prices households' problems are solved, and there are no arbitrage opportunities and markets for stocks clear,  $s_{t+1} = 1$ , in each interim period for all  $t = 0, 1, \dots$

### Lemma

*The optimality conditions that characterize the competitive equilibrium are*

$$q_t u'(c_t) \left(1 + \frac{\kappa \mu_t}{u'(c_t)}\right)^{-1} = \mathbb{E}_t [\beta u'(c_{t+1}) (q_{t+1} + d_{t+1})] \quad \text{and}$$
$$u'(c_t) - \mu_t = R_t \mathbb{E}_t [\beta u'(c_{t+1})]$$

where  $q_t^c$  is such that  $q_t u'(c_t) - \kappa \mu_t q_t^c = q_t^c u'(c_t)$ .

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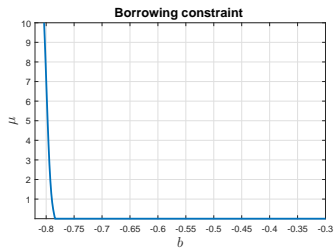
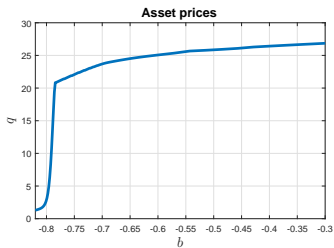
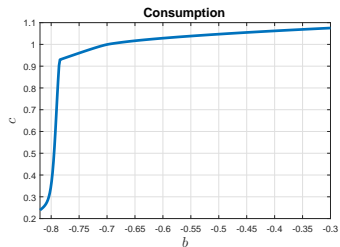
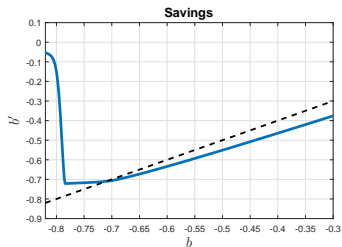
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- Fundamental trade-off between impatience and insurance when  $\beta R_t < 1$ .
- **Crisis:** constraint binds ( $\mu_t > 0$ )  $\rightarrow c_t \downarrow, q_t \downarrow$  and tightens constraint.
  - ▶ Feedback effect not internalized in competitive equilibrium
- External shocks  $\implies$  volatile capital flows.

# The Model

## Recursive Competitive Equilibrium

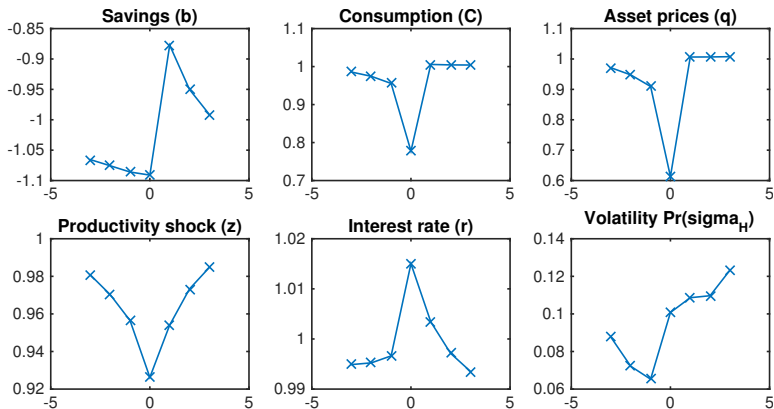


# Competitive Equilibrium

## Finding 1

1. Simulations of sudden stop episodes and the evolution of external shocks are consistent with the data.

► Reyes-Heroles and Tenorio (2016)

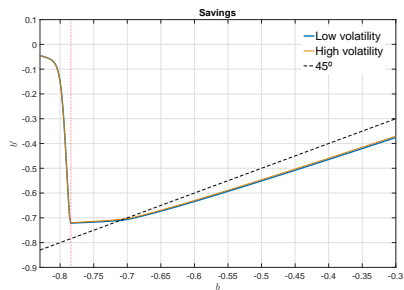
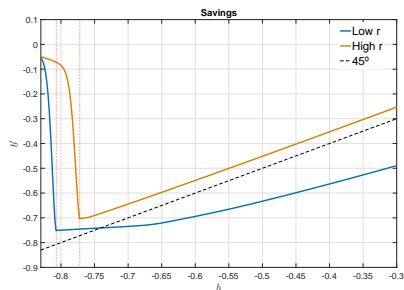


# Competitive Equilibrium

## Finding 2

- In the competitive equilibrium, allocations and prices are sensitive to external interest rate shocks, but not to their volatility.

► Fernández-Villaverde et al. (2011)



# The Model

## Constrained-Efficient Allocation

- Consider a social planner that internalizes externality on borrowing capacity and:
  - 1 Can choose aggregate debt, subject to economy's borrowing constraint,
  - 2 Cannot commit to future policies.
- Solve for constrained efficient allocations that a social planner would implement through time-consistent policies:
  - ▶ Following Klein et al. (2005, 2008) we restrict attention to time-consistent Markov policies:  $B' = \Psi(B, X)$ , where  $B$  is current aggregate debt and  $X$  is the vector of current exogenous shocks.
  - ▶ Focus on recursive formulation.

# The Model

## Constrained-Efficient Allocation

- **Assumption [Jeanne & Korinek (2010)]** Parameters and stochastic processes are such that the equilibrium pricing function satisfies  $1 + \kappa R(X) \psi(B, X) > 0$  where  $\psi(B, X) \equiv \partial \bar{Q}(B, \Psi(B, X), X) / \partial B$ . [▶ Formal Definition Q](#)

### Lemma

*The optimality condition that characterizes the constrained-efficient allocation is*

$$u'(C(B, X)) - \mu(B, X) = R(X) \beta \mathbb{E} [u'(C(B', X')) - \kappa \mu(B', X') \psi(B', X')]$$

*where  $\psi(B, X) = \partial \bar{Q}(B, \Psi(B, X), X) / \partial B$  and  $\mu(B, X)$  is the multiplier on the borrowing constraint.*

- Solution to the planner's problem  $\Leftrightarrow Q(B, X) = \bar{Q}(B, \Psi(B, X), X)$ .



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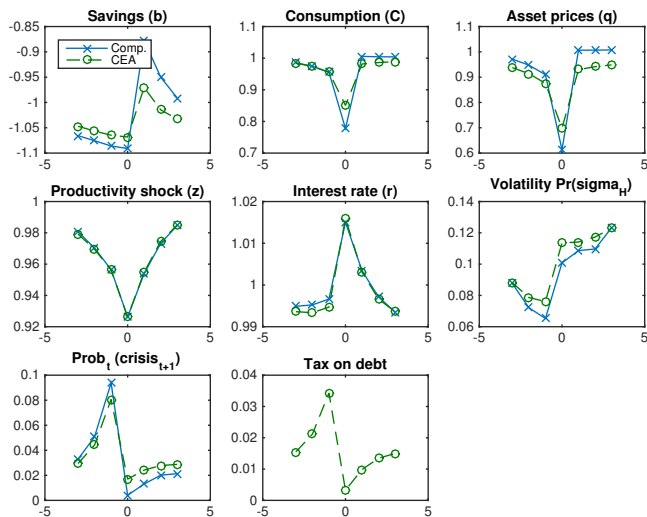
- Solution to the planner's problem  $\Leftrightarrow Q(B, X) = \bar{Q}(B, \Psi(B, X), X)$ .
- Implementation through macroprudential tax on external borrowing:

$$\tau(B, X) = \frac{\mathbb{E} [\kappa \psi(B', X') \mu(B', X') | X]}{\mathbb{E} [u'(C(B', X')) | X]}.$$

- Considers interaction of *severity*,  $\kappa \psi(B, X)$ , and *incidence*,  $\mu(B, X)$ , of potential future crises.

# The Model

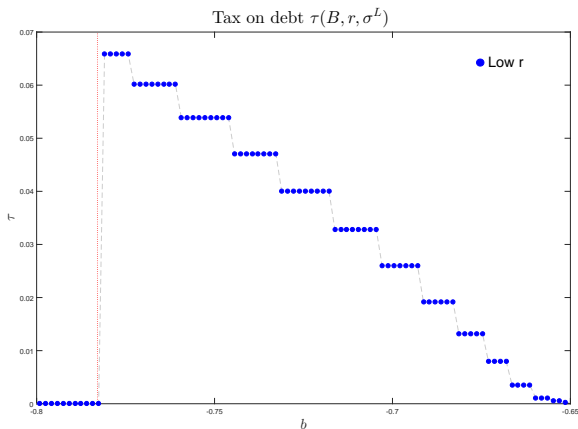
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## Findings 3 and 4

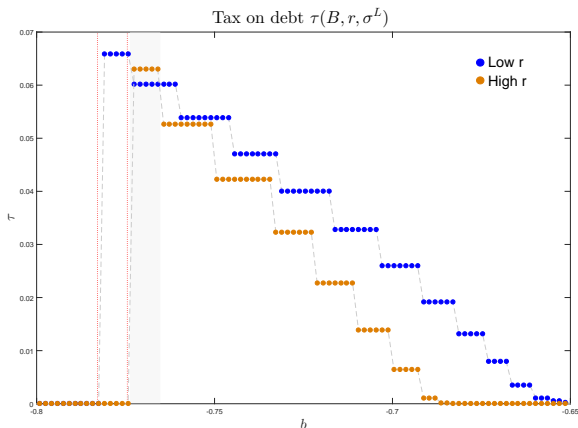
- Tax increasing in debt.



# Constrained-Efficient Allocation

## Findings 3 and 4

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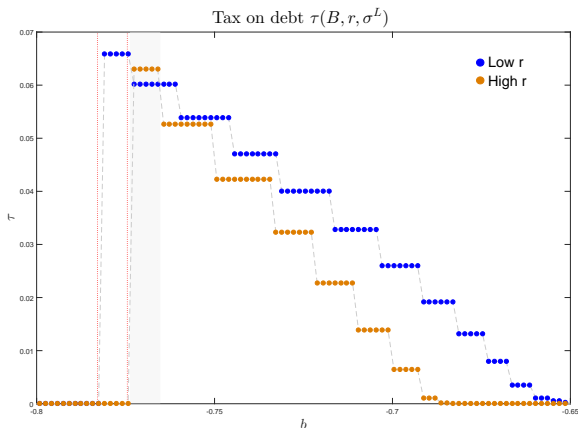


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$$\mathbb{E}[\kappa\psi(B', X')\mu(B', X')] = \mathbb{E}[\kappa\psi(B', X')] \cdot \mathbb{E}[\mu(B', X')] + Cov(\kappa\psi(B', X'), \mu(B', X'))$$

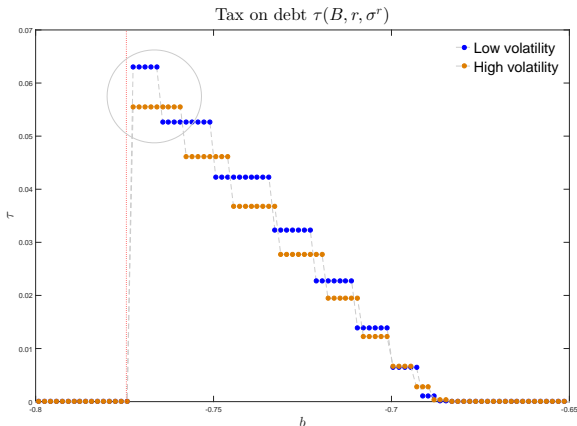


# Constrained-Efficient Allocation

## Findings 3 and 4

- Policy response to volatility shocks is non-monotonic → Changes in  $\mu$  effects are key: precautionary motives vs. price effects.

$$\mathbb{E}[\kappa\psi(B', X')\mu(B', X')] = \mathbb{E}[\kappa\psi(B', X')] \cdot \mathbb{E}[\mu(B', X')] + \text{Cov}(\kappa\psi(B', X'), \mu(B', X'))$$



# Conclusions

- Increases in external risks by themselves do not justify greater macroprudential intervention (e.g. capital controls) ⇒ *Important policy lesson!*
  - ▶ **Shocks to interest rate levels:** Clear message → consider effect of shocks on asset prices in crisis regions.
  - ▶ **Volatility shocks:** “Volatility paradox”
    - Relevant effect of volatility on asset prices (mechanism)
    - Individual precautionary saving motives have effects on particular regions of the state space
- Importance of considering the effects of external shocks on **asset prices** and their real implications (e.g. borrowing capacity).
  - ▶ Aggregate effects not internalized by private imply more room for macroprudential policy → influence borrowing decisions

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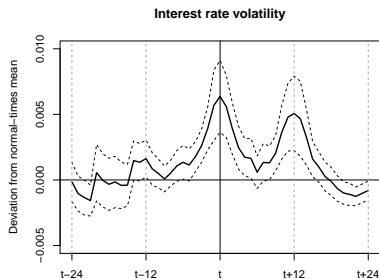
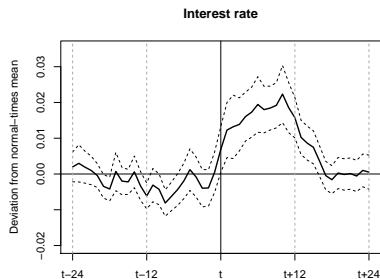


# Motivation and Question

## External Risks

- Neumeyer and Perri (2005), Uribe and Yue (2006) and Fernández-Villaverde et al. (2011)
- Reyes-Heroles and Tenorio (2017) using same data as previous work
  - ▶ Longstaff et al. (2011), Johri et al. (2015)

▶ Back



- a. Deviation of the interest rate from the normal-times country-specific mean (23 EMEs).
- b. Deviation of interest rate volatility from normal-times country-specific mean (23 EMEs). Interest rate volatility is measured as the seven-month centered moving standard deviation.  $t$  denotes the month in which the sudden stop begins. Dotted lines represent one standard error intervals.

# The Model

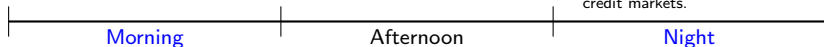
## Derivation of Collateral Constraint: Timing of Events

- Incentive compatibility constraint from limited enforcement problem.
- Recursive setup: state  $(b, s, B, X)$  given. HH's constraint:

- *Household*: chooses optimally  $(\hat{b}', \hat{s}', \hat{c})$  given  $Q$  and  $R$ .  
At this point  $\rightarrow \hat{c}$  is a plan.

- *Lender*: does not observe *Household's* actions.  
- *Household*: given  $(\hat{b}', \hat{s}', \hat{c})$   
 $\rightarrow$  can divert  $(1 - \kappa)\hat{s}'$  and decide to default.

- *Lender*: actions revealed to.  
 $\rightarrow$  confiscate  $\kappa\hat{s}'$  in country and sell for  $Q^c$  and lend at  $R$   
- *Household*: can choose final  $c$ , regain access to asset and credit markets.



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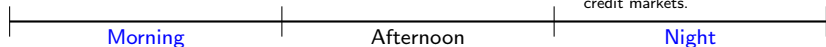
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$$V^a(\hat{c}, \hat{b}', \hat{s}', B, X) = \max \left\{ V^d(\hat{c}, \hat{b}', \hat{s}', B, X), V^r(\hat{c}, \hat{b}', \hat{s}', B, X) \right\}$$

$$V^m(b, s, B, X) = \max_{\hat{c}, \hat{b}', \hat{s}'} \left\{ V^a(\hat{c}, \hat{b}', \hat{s}', B, X) \right\}$$

$$\hat{c} + Q(B, X)\hat{s}' + \frac{\hat{b}'}{R(X)} = [Q(B, X) + d(X)]s + b$$

$$V^a(\hat{c}, \hat{b}', \hat{s}', B, X) = \max_{c, b', s'} \left\{ u(c) + \beta \mathbb{E} [V(b', s', B', X') | X] \right\}$$

$$d: c + Q^c(B, X)\hat{s}' + \frac{\hat{b}'}{R(X)} = (1 - \kappa) Q^c(B, X)\hat{s}' + \hat{c}$$

$$r: c + Q^c(B, X)\hat{s}' + \frac{\hat{b}'}{R(X)} = \frac{\hat{b}'}{R(X)} + Q^c(B, X)\hat{s}' + \hat{c}$$

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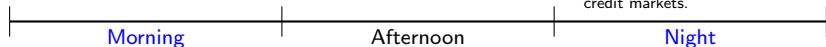
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- Incentive compatibility constraint from limited enforcement problem.
- Recursive setup: state  $(b, s, B, X)$  given. HH's constraint:

- *Household*: chooses optimally  $(\hat{b}', \hat{s}', \hat{c})$  given  $Q$  and  $R$ .  
At this point  $\rightarrow \hat{c}$  is a plan.

- *Lender*: does not observe *Household's* actions.  
- *Household*: given  $(\hat{b}', \hat{s}', \hat{c})$   
 $\rightarrow$  can divert  $(1 - \kappa)\hat{s}'$  and decide to default.

- *Lender*: actions revealed to.  
 $\rightarrow$  confiscate  $\kappa\hat{s}'$  in country and sell for  $Q^c$  and lend at  $R$   
- *Household*: can choose final  $c$ , regain access to asset and credit markets.



$$V^a(\hat{c}, \hat{b}', \hat{s}', B, X) = \max \{ V^d(\hat{c}, \hat{b}', \hat{s}', B, X), V^r(\hat{c}, \hat{b}', \hat{s}', B, X) \}$$

$$V^m(b, s, B, X) = \max_{\hat{c}, \hat{b}', \hat{s}'} \{ V^a(\hat{c}, \hat{b}', \hat{s}', B, X) \}$$

$$\hat{c} + Q(B, X)\hat{s}' + \frac{\hat{b}'}{R(X)} = [Q(B, X) + d(X)]s + b$$

$$V^a(\hat{c}, \hat{b}', \hat{s}', B, X) = \max_{c, b', s'} \{ u(c) + \beta \mathbb{E} [V(b', s', B', X') | X] \}$$

$$d: c + Q^c(B, X)s' + \frac{b'}{R(X)} = (1 - \kappa) Q^c(B, X)s' + \hat{c}$$

$$r: c + Q^c(B, X)s' + \frac{b'}{R(X)} = \frac{\hat{b}'}{R(X)} + Q^c(B, X)s' + \hat{c}$$

- To avoid diversion and default:  $-\frac{b'}{R(X)} \leq \kappa Q^c(B, X)s'$ .
- No arbitrage  $\Leftrightarrow Q(B, X)u'(\hat{C}(B, X)) - \kappa\mu(B, X)Q^c(B, X) = Q^c(B, X)u'(C(B, X))$ .

# Estimation and Calibration

Table: Baseline parameterization

Parameter		Value	Target
Time discount	$\beta$	0.96	Standard value
Relative risk aversion	$\gamma$	2	Standard value
Dividends	$d$	1	Normalization
Collateral constraint	$\kappa$	0.04	Debt-to-output ratio

- Result of estimation:

$$\begin{pmatrix} z_t \\ r_t \end{pmatrix} = \begin{pmatrix} 0.0052 \\ 0.0025 \end{pmatrix} + \begin{pmatrix} 0.6079 & -0.1321 \\ 0.1289 & 0.8261 \end{pmatrix} \begin{pmatrix} z_{t-1} \\ r_{t-1} \end{pmatrix} + \begin{pmatrix} \epsilon_t^z \\ \epsilon_t^r \end{pmatrix},$$

and the covariance and transition matrices are composed of:

$$\begin{aligned} \sigma^z &= 0.0312, & \rho &= -0.4048, & \pi_L &= 0.9610, \\ \sigma_L^r &= 0.0150, & \sigma_H^r &= 0.0661, & \pi_H &= 0.7468. \end{aligned}$$

# The Model

## Constrained-Efficient Allocation

### Lemma

Given an arbitrary future policy rule,  $\Psi(B, X)$  and the associated asset pricing function,  $Q(B, X)$ , the social planner solves

$$W(B, X) = \max_{c, B'} \{ u(c) + \beta \mathbb{E} [W(B', X) | X] \} \quad \text{s.t.}$$

$$c + \frac{B'}{R(X)} = d(X) + B,$$

$$\frac{B'}{R(X)} \leq \kappa \bar{Q}(B, B', X)$$

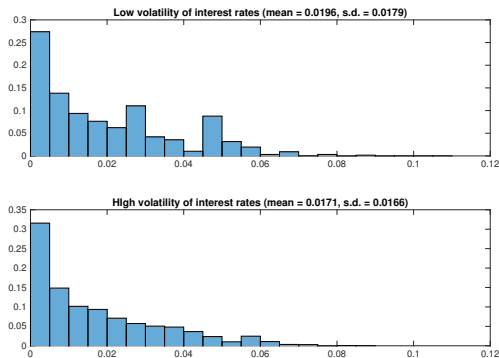
and the valuation of collateral is consistent with the household's trading of the stocks of the tree

$$\bar{Q}(B, B', X) = \beta \mathbb{E} \left[ \frac{u' \left( B' + d(X') - \frac{\Psi(B', X')}{R(X')} \right) (Q(B', X') + d(X'))}{u' \left( d(X) + B - \frac{B'}{R(X)} \right)} \middle| X \right].$$

# Constrained-Efficient Allocation

## Finding 4

- Should the planner intensify his intervention when external volatility increases? → Not necessarily.



Prevalence of  $\tau = 0$ : Low Volatility → 55.3%, High Volatility → 59.6%.

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# Constrained-Efficient Allocation

## Findings 3 and 4

- Decomposition of optimal tax.

